References

- ANDO, K., MURAKAMI, Y. & NAWATA, Y. (1971). J. Antibiot. (Tokyo), 24, 418-422.
- ANDO, K., OISHI, H., HIRANO, S., OKUTOMI, T., SUZUKI, K., OKAZAKI, H., SAWADA, M. & SAGAWA, T. (1971). J. Antibiot. (Tokyo), 24, 347–352.
- DOBLER, M. (1972). Helv. Chim. Acta, 55, 1371-1384.
- DOMINGUEZ, J., DUNITZ, J. D., GERLACH, H. & PRELOG, V. (1962). *Helv. Chim. Acta*, **45**, 129–138.
- DUAX, W. L., HAUPTMAN, H., WEEKS, C. M. & NORTON, D. A. (1972). Science, 176, 911–914.
- GRAVEN, S. N., LARDY, H. A. & ESTRADA-O., S. (1967). Biochemistry, 6, 365-371.
- IITAKA, Y., SAKAMAKI, T. & NAWATA, Y. (1972a). Acta Cryst. A28, S47.
- IITAKA, Y., SAKAMAKI, T. & NAWATA, Y. (1972b). Chem. Lett. (Tokyo), pp. 1225–1230.
- International Tables for X-ray Crystallography (1962). Vol. III, pp. 202–203. Birmingham: Kynoch Press.
- JOHNSON, C. K. (1965). ORTEP. Report ORNL-3794, Oak Ridge National Laboratory, Oak Ridge, Tennessee, USA.

- KARLE, J. & KARLE, I. J. (1966). Acta Cryst. 21, 849-859.
- KYOGOKU, Y., AKUTSU, H., KOBAYASHI, Y., KAWANO, K. & UENO, M. (1973). The 12th Symposium on NMR Spectroscopy, Hiroshima, Japan.
- LUTZ, W. K., WINKLER, F. K. & DUNITZ, J. D. (1971). Helv. Chim. Acta, 54, 1103-1108.
- MATSUZAKI, T. & IITAKA, Y. (1971). Acta Cryst. B27, 507-516.
- MUELLER, P. & RUDIN, D. O. (1967). Biochem. Biophys. Res. Commun. 26, 398–404.
- OGATA, E. & RASMUSSEN, H. (1966). Biochemistry, 5, 57-66.
- OKAYA, Y. & ASHIDA, T. (1967). *HBLS* IV, The Universal Crystallographic Computing System (I), p. 65, Japanese Crystallographic Association.
- POPLE, J. A. (1962). J. Chem. Phys. 37, 60-66.
- PRESTEGARD, J. H. & CHAN, S. I. (1969). Biochemistry, 8, 3921-3927.
- PRESTEGARD, J. H. & CHAN, S. I. (1970). J. Amer. Chem. Soc. 92, 4440–4446.
- UENO, M., AKUTSU, H., KYOGOKU, Y. & NAWATA, Y. (1973). The 12th Annual Meeting of the Biophysical Society of Japan, Tokyo.

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The High-Temperature Structure of CsCuCl₃

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The crystal structure of CsCuCl₃, above its transition temperature (423 °K) has been determined at 466 °K. The polar hexagonal space group $P6_{3}mc$ is the most probable one for this compound. The cell dimensions are a = 7.245 (7) and c = 6.150 (6) Å with Z = 2. Full-matrix least-squares refinement of 185 observed symmetry-independent three-dimensional diffractometer data (Mo $K\alpha$) led to a final R index on F of 0.041 and a weighted R index of 0.069. Above its transition temperature CsCuCl₃ is isostructural with CsCrCl₃ and CsCrBr₃. The Cu²⁺ ion is slightly displaced from the centre of a Cl⁻ octahedron along the trigonal axis (c axis) giving rise to a ferroelectric structure.

Introduction

In a previous communication (Kroese, Tindemans-van Eyndhoven & Maaskant, 1971) we reported a phase transition in CsCuCl₃ at 423 °K; we also discussed the high-temperature structure as determined by single-crystal Weissenberg measurements. However, owing to the lack of sufficient data we could not determine unequivocally the space group of this compound. In order to solve this problem we performed single-crystal X-ray diffractometer measurements, the results of which are communicated here.

Experimental

Crystals of CsCuCl₃ were grown from an aqueous solution as described elsewhere (Schlueter, Jacobson &

Rundle, 1966). An irregularly shaped crystal of approximate size $0.2 \times 0.2 \times 0.6$ mm was mounted on an Enraf–Nonius three-circle single-crystal diffractometer with the hexagonal axis along the φ -axis. The diffractometer was equipped with an apparatus enabling us to heat the crystal with a continuous stream of hot nitrogen gas. The temperature of the crystal during the experiment was $466 \pm 5^{\circ}$ K. Precise unit-cell parameters were determined at this temperature by measuring nine carefully selected reflexions with Zr-filtered Mo $K\alpha$ radiation ($\lambda = 0.71069$ Å). The cell parameters are: a=7.245 (7), c=6.150 (6) Å (numbers in parentheses here and in the tables are estimated standard deviations in the least significant digit). The calculated density at 466°K for Z=2 and a molecular weight of 302.8, d=3.63 g cm⁻³, agrees with the measured density at room temperature, d=3.65 g cm⁻³. Intensities were

recorded by the θ -2 θ scan method for all reflexions with θ between 4 and 30° using Zr-filtered Mo K α radiation. The scan angle Δ was 1.7°. The counting time was 41 s for each background and 82 s for the scan. In all 1039 reflexions were measured. The standard deviations σ_F were calculated from the statistical inaccuracy of the measurement with an amount added for errors in the absorption correction and attenuation factors. Reflexions with intensity less than twice the standard deviation were considered not significant.

All data were corrected for absorption,* Lorentz and polarization effects. The transmission factors ranged between 0.20 and 0.28 ($\mu = 119.7$ cm⁻¹).

Determination of the structure

The crystal belongs to the hexagonal Laue group 6/mmm. Together with the systematic absences hh2hl, l=2n+1 this indicates one of the following space groups: $P6_3/mmc$, $P\overline{6}2c$ or $P6_3mc$. Models having these space groups were refined by a full-matrix least-squares method. Scattering factors for Cs⁺, Cu²⁺ and Cl⁻ and anomalous dispersion corrections ($\Delta f'$ and $\Delta f''$) for Cs⁰, Cu⁰ and Cl⁰ were taken from the compilation of Cromer & Waber (1965). All intensities were reduced to F values and an averaging procedure was carried out for each space group giving only symmetryindependent reflexions: only the significant reflexions were used in the refinement. The function minimized during the least-squares refinement process was: $\sum w_F(|F_o| - |F_c|)^2$ with the weighting factor $w_F = 1/(\sigma_F)^2$. Discrepancy indices referred to are:

and

$$R_{wF} = \left[\frac{\sum w_F(|F_o| - |F_c|)^2}{\sum w_F|F_c|^2}\right]^{1/2}$$

 $R_F = \frac{\sum ||F_o| - |F_c||}{\sum |F_o|}$

Assuming 2 molecules per unit cell the possible positions for the atoms in the three space groups can easily

* All calculations were carried out on the Leiden University I.B.M. 360/50 and later on the 360/65 computer using programs written or modified by Mrs Rutten-Keulemans and Mr De Graaff of the section X-ray and electron diffraction. be found in *International Tables for X-ray Crystallography* (1952); they are given in Table 1.

Table 1. Positions for the atoms in the different space groups

	Р	63/1	ттс	•		РĞ	2 <i>c</i>		$P6_3mc$						
Cs Cu Cl	(d) (a) (h)	$\frac{1}{3}$ 0 x		$ \frac{\frac{3}{4}}{\frac{1}{4}} $	(d) (a) (h)	$\frac{1}{3}$ 0 x	23 0 y	34 0 14	(b) (a) (c)			z z z			

The positional parameters and anisotropic thermal parameters for all atoms and a scaling factor were refined. In the refinement of the model with space group $P6_{3}mc$ the z coordinate of the Cs atom was set at $\frac{3}{4}$.

The final discrepancy indices for the refinements are given in Table 2. The estimated standard deviations of an observation of unit weight (ERF) given by $\left[\sum w_F(|F_o| - |F_c|)/(NO - NV)\right]^{1/2}$ (where NO is the number of observations and NV is the number of variables) are also given in Table 2. The values are probably high owing to systematic errors in the absorption correction, which had to be carried out for an imaginary crystal form that corresponded with the measured transmission curve for the main reflexions 002 and 004, because the shape of the single crystal was too irregular. The errors in the absorption correction are also thought to be the explanation for some positive and negative peaks around the threefold axes of the system in the final difference Fourier synthesis. Least-squares refinements for all three models were also carried out with the set of 145 symmetry-independent reflexions of the space group $P6_3/mmc$. The final discrepancy indices for these refinements are also given in Table 2. When we apply Hamilton's (1965) statistical test to these R indices we find that the possibility of $P6_3/mmc$ or $P\overline{6}2c$ being the

Table 2. Final discrepancy values

	R_f	R_{wf}	Number of reflexions	Number or parameters	ERF
$P6_3/mmc$	0.059	0.101*	145	9	10.81
P62c	0.066	0.105	276	11	7.80
	0.029	0.100*	145	11	10.84
P6₃mc	0.041	0.069	185	12	6.54
-	0.046	0.068*	145	12	7.32

* Values used with Hamilton's test.

Table 3. Positional and thermal parameters for
$$CsCuCl_3(466 \,^{\circ}K)$$
 with the space group $P6_3$ mc

The general anisotropic temperature factor has the form $[\exp -2\pi^2(\sum_{i,j} U_{ij}a_i^*a_j^*)]$.

Owing to the site symmetry of the ions there are several restrictions on the thermal parameters U_{ij} :

Cu, Cs:
$$U_{11} = U_{22} = 2U_{12}$$

Cl: $U_{22} = 2U_{12}$
 $U_{13} = U_{23} = 0$
 $2U_{13} = U_{23}$

All parameters not given as fractions are multiplied by 10³.

	x	У	z	U_{11}	U_{22}	U_{33}	$2U_{12}$	$2U_{23}$	$2U_{13}$
Cs	ł	23	3	52 (1)	52 (1)	92 (2)	52 (1)	0	0
Cu	Ō	Ō	15 (6)	65 (1)	65 (1)	44 (2)	65 (1)	0	0
Çl	152 (3)	304 (6)	280 (15)	59 (2)	70 (3)	116 (6)	70 (3)	36 (14)	18 (7)

right space group can be rejected on a significance level less than 0.5 %. So on this basis of the statistical test we conclude that the structure of CsCuCl₃ at 466 °K (*i.e.* above its transition temperature) has the polar space group $P6_3mc$ with parameters as given in Table 3. A list of structure factors can be found in Table 4.

Our calculations show that CsCuCl₃ above its transition temperature is not isostructural with CsNiCl₃ (Tishchenko, 1955) and CsMgCl₃ (McPherson, Kistenmacher & Stucky, 1970) the main difference being that the centre of inversion on the Cu²⁺ ion is lacking. The coordination about the Cu²⁺ ion is no longer octahedral with a slight trigonal distortion (site symmetry D_{3d}): the Cu²⁺ ion is displaced along the *c* axis towards a shared face. This results in a lowering of the site

Table 4. List of structure factors $\times 10$

F(0,0,0) on this scale is 2706.

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Fig. 1. A perspective view of the anionic chain of CsCuCl₃.

symmetry from D_{3d} to C_{3v} and also in the possibility of different Cu–Cl distances.

In fact we determined three shorter distances of 2.39 (1) Å and three larger distances of 2.51 (1) Å but in reality the difference between the distances may be smaller. A list of nearest-neighbour bond lengths and relevant angles is given in Table 5. The distances and angles are indicated in Fig. 1.

Table 5. Interionic distances (Å) and bond angles and their estimated standard deviations

The e.s.d.'s include the e.s.d.'s in the cell parameters.

Dist	tances	Bond a	Bond angles							
Cu-Cl	2.51 (1)	Cl-Cu-Cl	82.5 (4)							
Cu–Cl′	2.39 (1)	Cl'-Cu-Cl'	87·2 (5)							
Cl-Cl	3.30 (1)		. ,							
Cl–Cl′	3.619 (4)	Cl–Cu–Cl′	95.1 (2)							
Cs-Cl	3.68 (1)	Cu-Cl-Cu	77.7 (2)							
CsCl'	3.632 (4)		. ,							

With the parameters given in Table 3 and assuming a point-charge model we can calculate a spontaneous polarization $P_s = -4.2 \times 10^{-2}$ C m⁻² for CsCuCl₃ at 466°K. In order to check the results of the structure determination independently polarization measurements were made but no conclusive evidence for the polarity or non-polarity of the space group could be obtained.

A possible explanation for the ferroelectric behaviour may be the following: owing to the lowering of the symmetry of the ions, especially Cl^- and Cu^{2+} , more orbitals can be involved in the copper-chlorine binding giving rise to asymmetrical charge distribution and hence to polarization. The increase in polarization energy may stabilize this structure. A rough qualitative MO picture of the copper-chlorine bonding in this compound seems to indicate that such polarization effects can indeed lower the energy.

Recently the structure determinations of CsCrCl₃ (McPherson, Kistenmacher, Folkers & Stucky, 1972) and of CsCrBr₃ (Li & Stucky, 1973) have been published. It is interesting to compare the results of these structure determinations with ours. It is stated in both cases that the most probable space group at room temperature is $P6_3mc$ in agreement with our findings in CsCuCl₃ at 466°K. The Cr–Cl distances are 2.419(5) and 2.618(6) Å in CsCrCl₃ and 2.574(12) and 2.780 (13) Å in CsCrBr₃. It is remarkable that three CsMCl₃ compounds with M a Jahn-Teller active ion exhibit this particular structure. In CsCrCl₃ and CsCrBr₃ Stucky and his coworkers found a great deal of anisotropic motion along the c axis which they think arises from a Jahn-Teller effect. In Table 6 we give the root-mean-square amplitudes of vibration along the principal axes and it can be seen (Fig. 1), that in our case too there is some anisotropy in thermal motion along the c axis for the chlorine ion. The similarity in behaviour of these three compounds should in our

Table 6. Root-mean-square amplitudes of vibration along the principal axes

Direction cosines are with respect to an orthogonal axis system: $x \perp \mathbf{b}$, $y \parallel \mathbf{b}$, $z \parallel \mathbf{c}$

	$(\overline{u^2})^{1/2}$ (Å)		cosines		$(\overline{u^2})^{1/2}$		cosines		$(\overline{u^2})^{1/2}$		cosines	5
Cs	0.30	0	0	1	0.23	1	0	0	0.23	0	1	0
Cu	0.21	0	0.	1	0.25	1	0	0	0.22	0	1	0
Cl	0.35	0.17	0.29	0 ∙94	0.23	0· 87	-0.50	0	0.25	0 ∙47	0.85	-0.33

opinion clearly be ascribed to the Cu^{2+} and Cr^{2+} ions: both have an orbitally degenerate ground state and can be Jahn–Teller active.

Having seen the close resemblance in behaviour between $CsCuCl_3$ and $CsCrCl_3$ and $CsCrBr_3$ one might wonder if the latter two compounds exhibit a phase transition to a structure with space group $P6_122$ (roomtemperature space group of $CsCuCl_3$) at a temperature below 293 °K. As far as we know no such behaviour has been reported in the literature.

At present we are preparing a publication on the connexion between the low-temperature structure of CsCuCl₃ and the structure with space group $P6_3/mmc$. Natarajan & Prakash (1971) state in an article on phase transitions in ABX₃ type halides that the structure of CsCuCl₃ changes from hexagonal to cubic at the transition point. Our calculations, as reported here, prove this statement wrong.

We thank Mrs J. C. M. Tindemans-van Eyndhoven for assistance in the experimental part of the investigation. The investigations were supported in part by the Netherlands Foundation for Chemical Research (S.O.N.) with financial aid from the Netherlands Organization for the Advancement of Pure Research (Z.W.O.).

References

- CROMER, D. T. & WABER, J. T. (1965). Acta Cryst. 18, 104– 109.
- HAMILTON, W. C. (1965). Acta Cryst. 18, 502-510.
- International Tables for X-ray Crystallography. (1952). Vol. I, pp. 293, 297, 304, Birmingham: Kynoch Press.
- KROESE, C. J., TINDEMANS-VAN EYNDHOVEN, J. C. M. & MAASKANT, W. J. A. (1971). Solid State Commun. 9, 1707–1709.
- LI, T. & STUCKY, G. D. (1973). Acta Cryst. B29, 1529-1532.
- MCPHERSON, G. L., KISTENMACHER, T. J., FOLKERS, J. B. & STUCKY, G. D. (1972). J. Chem. Phys. 57, 3771–3780.
- MCPHERSON, G. L., KISTENMACHER, T. J. & STUCKY, G. D. (1970). J. Chem. Phys. 52, 815–824.
- NATARAJAN, M. & PRAKASH, B. (1971). Phys. Stat. Sol. (a), 4, K167-K172.
- SCHLUETER, A. W., JACOBSON, R. A. & RUNDLE, R. E. (1966). *Inorg. Chem.* 5, 277–280.
- TISHCHENKO, G. N. (1955). Tr. Inst. Kristallogr. Akad. Nauk SSSR, 11, 93-96.

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Structure Cristalline et Moléculaire du 2-S-Ethyl-2-thio-D-mannose Diéthyl Dithioacétal

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(Reçu le 16 novembre 1973, accepté le 12 décembre 1973)

The crystal structure of 2-S-ethyl-2-thio-D-mannose diethyl dithioacetal ($C_{12}H_{26}O_4S_3$) has been determined by three-dimensional X-ray analysis. The crystals are monoclinic, a=15.733, b=7.214, c=16.885 Å, $\beta=113.23^{\circ}$ and Z=4, space group $P2_1$. The intensities were measured with a four-circle diffractometer using Mo K α radiation. The structure was solved by a modification of the symbolic addition procedure, based on the introduction of the phase function. The stereochemistry at C(2) is manno and the sulphur atoms present very short intramolecular contacts. The carbon chain adopts the extended planar zigzag.

Introduction

Les travaux de Horton et collaborateurs (Horton & Miller, 1965; Horton & Wander, 1969) sur les conformations de sucres acycliques par RMN ont mis en évidence leur conformation plane en zigzag lorsqu'il n'existe pas d'interactions stériques entre les substituants portés par des carbones en position alternée. Cette hypothèse a été confirmée dans le cas d'une série d'alditols, par une étude aux rayons X (Jeffrey & Kim,